

# CASIO®

## fx-991ZA PLUS II

### TABLE & STAT MODE

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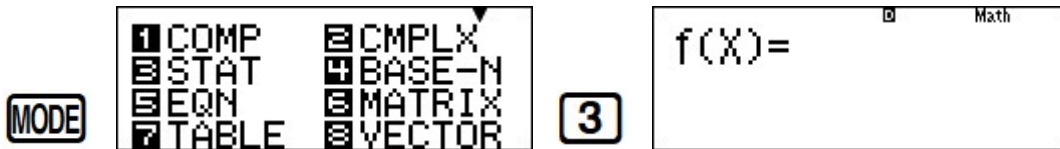
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## MODE 7: TABLE



### A. GENERATE TABLES TO SKETCH GRAPHS

1.  $y = 2x + 3$                        $-1 \leq x \leq 3$

<ul style="list-style-type: none"> <li>• Input <math>f(x)</math> formula  <math>f(x) = 2x + 3</math> to input the variable <math>x</math>:  <math>x</math></li> <li>• <math>g(x) =</math> </li> </ul> <p>And the co-ordinates to plot are: (-1 ; 1) (0 ; 3) (1 ; 5) (2 ; 7) (3 ; 9)</p>	<ul style="list-style-type: none"> <li>• Set boundaries for your table: Start?  <math>1</math> </li> <li>End? <math>3</math> </li> <li>Step? <math>1</math> </li> </ul>
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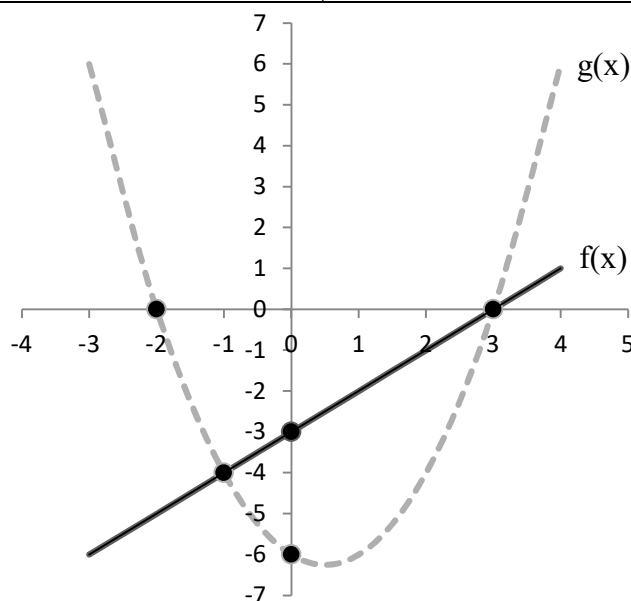
**Remember:** returns you to the formula

**2. Find the points of intersection of the straight-line  $f(x) = x - 3$  and the parabola  $g(x) = x^2 - x - 6$  when  $x \in [-3 ; 4]$**

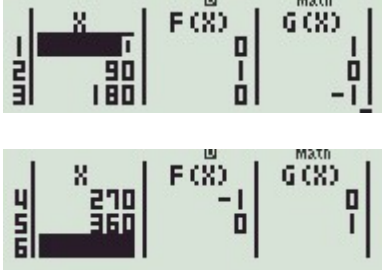
<p><b>Key Sequence:</b></p> <ul style="list-style-type: none"> <li>• Input <math>f(x)</math> formula <math>\text{=}</math></li> <li>• Input <math>g(x)</math> formula <math>\text{=}</math></li> <li>• Set boundaries for the table:              Start? <math>\leftarrow</math> <math>3</math> <math>\text{=}</math>              End? <math>4</math> <math>\text{=}</math>              Step? <math>1</math> <math>\text{=}</math></li> </ul> <p><b>Point of Intersection (-1 ; -4)</b></p> <p><b>Point of Intersection (3 ; 0)</b></p>	<p><b>On screen:</b></p> <p><math>f(X)=X-3</math></p> <p><math>g(X)=X^2-X-6</math></p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr><td colspan="4">Math</td></tr> <tr><td>X</td><td>F(X)</td><td colspan="2">G(X)</td></tr> <tr><td>-3</td><td>-6</td><td>-6</td><td>-6</td></tr> <tr><td>-2</td><td>-5</td><td>-4</td><td>-6</td></tr> <tr><td>-1</td><td>-4</td><td>-2</td><td>-6</td></tr> <tr><td>0</td><td>-3</td><td>0</td><td>-6</td></tr> <tr><td>1</td><td>-2</td><td>2</td><td>-6</td></tr> <tr><td>2</td><td>-1</td><td>4</td><td>-6</td></tr> <tr><td>3</td><td>0</td><td>6</td><td>-6</td></tr> <tr><td>4</td><td>1</td><td>8</td><td>-6</td></tr> </table>	Math				X	F(X)	G(X)		-3	-6	-6	-6	-2	-5	-4	-6	-1	-4	-2	-6	0	-3	0	-6	1	-2	2	-6	2	-1	4	-6	3	0	6	-6	4	1	8	-6
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-1	-4	-2	-6																																						
0	-3	0	-6																																						
1	-2	2	-6																																						
2	-1	4	-6																																						
3	0	6	-6																																						
4	1	8	-6																																						

**\* ZOOM IN \* and find the turning point of  $g(x)$**

<p><b>Key Sequence:</b></p> <ul style="list-style-type: none"> <li>• <math>\text{AC}</math></li> <li>• Change the boundaries of the table              Start? <math>0</math> <math>\text{=}</math>              End? <math>1</math> <math>\text{=}</math>  <b>Reduce the STEPS/INTERVALS for a more detailed table.</b>              Step? <math>\cdot</math> <math>2</math> <math>5</math> <math>\text{=}</math></li> </ul> <p><b>Turning point of <math>g(x)</math>: (0,5 ; -6,25)</b></p>	<p><b>On screen:</b></p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr><td colspan="4">Math</td></tr> <tr><td>X</td><td>F(X)</td><td colspan="2">G(X)</td></tr> <tr><td>0</td><td>-3</td><td>-6</td><td>-6</td></tr> <tr><td>0.25</td><td>-2.75</td><td>-6.187</td><td>-6</td></tr> <tr><td>0.5</td><td>-2.5</td><td>-6.25</td><td>-6</td></tr> </table> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr><td colspan="4">Math</td></tr> <tr><td>X</td><td>F(X)</td><td colspan="2">G(X)</td></tr> <tr><td>0.75</td><td>-2.25</td><td>-6.187</td><td>-6</td></tr> <tr><td>1</td><td>-2</td><td>-6</td><td>-6</td></tr> </table>	Math				X	F(X)	G(X)		0	-3	-6	-6	0.25	-2.75	-6.187	-6	0.5	-2.5	-6.25	-6	Math				X	F(X)	G(X)		0.75	-2.25	-6.187	-6	1	-2	-6	-6
Math																																					
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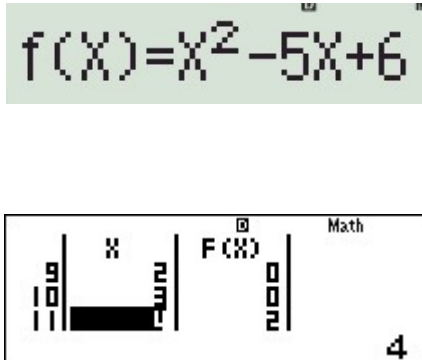
**3. Compare:**  $y = \sin x$  and  $y = \cos x$   $x \in [0^\circ ; 360^\circ]$

<p><b>Key Sequence:</b></p> <ul style="list-style-type: none"> <li>• Input <math>f(x)</math> formula <math>\equiv</math></li> <li>• Input <math>g(x)</math> formula <math>\equiv</math></li> <li>• Set boundaries for your table:              Start? <math>0 \equiv</math>              End? <math>3 \ 6 \ 0 \equiv</math></li> </ul> <p><b>You need to carefully select the STEPS (or INTERVALS) for your graph.</b>  <b>Consider the equations as a guideline.</b>              Step? <math>9 \ 0 \equiv</math></p>	<p><b>On screen:</b></p> <p><math>f(X)=\sin(X)</math>   <math>g(X)=\cos(X)</math></p> 
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## B.SOLVING EQUATIONS IN TABLE MODE

Quadratic equation  $x^2 - 5x + 6 = 0$

Generate a TABLE for the equation & read off the  $x$  value where  $f(x) = 0$

<p><b>Key Sequence:</b></p> <ul style="list-style-type: none"> <li>• Input <math>f(x)</math> equation <math>\equiv</math>  <b>to input the variable <math>x</math>:</b>  <math>\text{ALPHA} \ ]</math></li> <li>• <math>g(x) =</math> <math>\equiv</math></li> <li>• Set boundaries for your table:              Start? <math>- \ 6 \equiv</math>              End? <math>6 \equiv</math>              Step? <math>1 \equiv</math></li> </ul> <p><math>f(x) = 0</math> at <math>x = 2</math> or <math>x = 3</math></p>	<p><b>On screen:</b></p> <p><math>f(X)=X^2-5X+6</math></p> 
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*DOMAIN: Negative & positive values of the constant*  
*STEPS: Reciprocal / Inverse of the co-efficient of the highest power of x*

*DON'T FORGET*  
 $f(x)$  &  $g(x) - 20$   $x$  values  
 $f(x) - 30$   $x$  values

*HOW TO CHANGE:*

1:ab/c	2:d/c	Select Type? 1: f(x) 2: f(x), g(x)
3:CMPLX	4:STAT	
5:TABLE	6:APO	
7:CONT		

$\text{SHIFT} \ \text{MODE} \ \downarrow$     $\boxed{4}$

# STATISTICS

“The practice of collecting and analysing numerical data in large quantities”

Wikipedia

## MODE 3: Statistics



1. Single variable / Data handling
2. Linear regression
3. Quadratic regression
4. Logarithmic regression
5. Exponential regression
6. AB exponential regression
7. Power regression
8. Inverse regression

### 1. SINGLE VARIABLE DATA HANDLING

#### 1: 1-VAR

##### A. Ungrouped Data

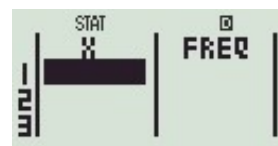
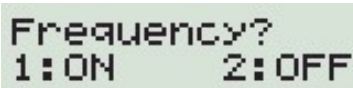
The following data set represents the March rainfall figures (in mls) for the past 12 years for a South African town:

77    75    68    81    110    90    81    42    68    81    95    72

**NOTE:** some of the values have been repeated - **It is useful to have the frequency table on**

How to set up a frequency table:

SHIFT MODE  $\blacktriangledown$  4 1



The frequency table helps:

- to determine mode easily
- to group the data and therefore accommodate more values

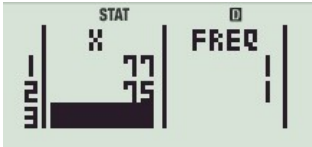


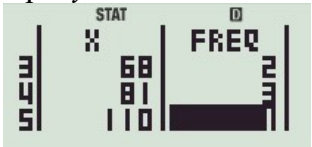
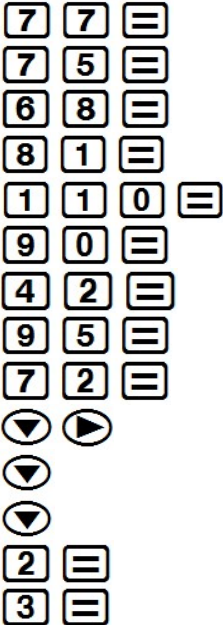
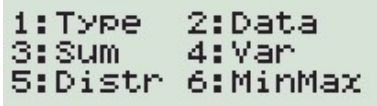
Using your calculator find:

#### MEASURES OF CENTRAL TENDENCY / AVERAGES

1. **MEAN:** sum of values divided by the number of values
2. **MODE:** value which occurs most often
3. **MEDIAN:** the central number of a data set

## MEASURE OF DISPERSION / SPREAD AROUND THE AVERAGE

4. **RANGE:** highest value *minus* lowest value
5. **QUARTILES:** measure the spread of values above and below the mean by dividing the distribution into four groups.
6. **STANDARD DEVIATION:** measure of dispersion around the mean
7. **VARIANCE:** standard deviation squared

Solution:	Key Sequence:
Set your calculator to Stats mode for Univariate data	<b>MODE</b> <b>3</b> <b>1</b>
Enter the data into the table: Input all the <i>x</i> -values first   Use the  arrows to move the cursor to the top of the <i>y</i> -column. Input <i>y</i> -values 	
Clear the screen - ready for the <b>Single variable sub menu</b> 	<b>AC</b> <b>SHIFT</b> <b>1</b>


### Breakdown of **Single variable sub menu**

Key	Menu Item	Explanation
1: Type	Stats menu	Change statistical calculation type
2: Data		Displays inputted data
3: Sum	<b>1: <math>\Sigma x^2</math>    2: <math>\Sigma x</math></b>	1. Sum of squares 2. Sum
4: Var	<b>1: <math>n</math>        2: <math>\bar{x}</math> 3: <math>\sigma x</math>    4: <math>s x</math></b>	1. Number of samples 2. Mean <b>3. Population standard deviation</b> 4. Sample standard deviation
5: Distr		Perform normal distribution calculations
6: MinMax	<b>1: minX    2: maxX 3: Q1      4: med 5: Q3</b>	1. Minimum value 2. Maximum value 3. First quartile 4. Median 5. Third quartile

1. MEAN

**SHIFT** **1** **4** **2** **=**  $\bar{x}$  =

2. MODE

**AC** **SHIFT** **1** **2** Find the highest frequency  =

3. MEDIAN

**AC** **SHIFT** **1** **6** **4** **=** 4:med =

4. RANGE

**AC** **SHIFT** **1** **6** **2** **-** **SHIFT** **1** **6** **1** **=** maxx-minx =

5. QUARTILES

**AC** **SHIFT** **1** **6** **3** **=** Q1 =


**AC** **SHIFT** **1** **6** **5** **=** Q3 =


*Using the five-number summary (maximum, minimum, median & quartiles) you can draw a box and whisker diagram.*

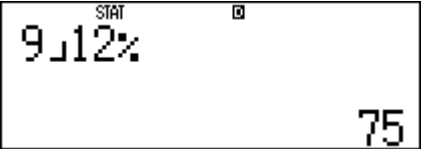
6. STANDARD DEVIATION (POPULATION)

**AC** **SHIFT** **1** **4** **3** **=**  $\sigma_x$  =

**DETERMINE THE PERCENTAGE OF THE RAINFALL FIGURES WITHIN ONE STANDARD DEVIATION FROM THE MEAN.**

**AC** **SHIFT** **1** **4** **2** **-** **SHIFT** **1** **4** **3** **=** 

**AC** **SHIFT** **1** **4** **3** **=** 

**AC** **9** **=** **1** **2** **SHIFT** **(** **=** 

**(** **77** **)** **(** **75** **)** **(** **68** **)** **(** **81** **)** **(** **110** **)** **(** **90** **)** **(** **81** **)** **(** **42** **)** **(** **68** **)** **(** **81** **)** **(** **95** **)** **(** **72** **)**

## B. Grouped Data

When data is grouped it is first necessary to find a single value to represent each class. This single value is the midpoint of the interval.

➤ Suppose you asked a group of men to count the number of items in their pockets.

**NOTICE:**

- The data items in the table below are groups, so first you need to find the **midpoints of the groups**.

Notice that the numbers 0, 1, 2, 3 and 4 are included in the group 0 – 4. The middle score is thus 2.

a) First calculate the midpoint  $\bar{X}$  of each of the groups

No of items	Frequency
0 – 4	6
5 – 9	11
10 – 14	6
15 – 19	4
20 – 24	3
	$n = 30$

Midpoint of groups
2
7

b) Input the data into the calculator – AS SHOWN IN THE PREVIOUS EXAMPLE.

c) Calculate the value of the mean.

$$\boxed{\text{SHIFT}} \boxed{1} \boxed{4} \boxed{2} \boxed{=}$$

$$\bar{x} =$$

d) Find the Standard Deviation correct to 2 decimal places.

$$\boxed{\text{AC}} \boxed{\text{SHIFT}} \boxed{1} \boxed{4} \boxed{3} \boxed{=}$$

$$\sigma_x =$$

### How to set your calculator to round off to 2 decimal places

1:MthIO 2:LineIO 3:Deg 4:Rad 5:Gra 6:Fix 7:Sci 8:Norm	<b>Key Sequence:</b> $\boxed{\text{SHIFT}} \boxed{\text{MODE}} \boxed{6}$ Now select decimal places $\boxed{2}$	Fix 0~9?
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### How to clear your calculator from rounding off to 2 decimal places

1:MthIO 2:LineIO 3:Deg 4:Rad 5:Gra 6:Fix 7:Sci 8:Norm	<b>Keys Sequence:</b> $\boxed{\text{SHIFT}} \boxed{\text{MODE}} \boxed{8}$ Select $\boxed{2}$	Norm 1~2?
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Norm 1 is the **default setting** and gives answers in scientific notation.

e.g.  $1 \div 50\,000 = 2 \times 10^{-5}$

Norm 2 is **generally preferred** as answers are only expressed in scientific notation when they are too big to fit on the screen.

e.g.  $1 \div 50\,000 = 0.00002$

## 2. LINEAR REGRESSION

$$Y = A + BX$$

**Linear Regression** predicts a relationship between a dependent variable ( $y$ ) and an independent variable ( $x$ )

Where the relationship approaches that of a straight line.

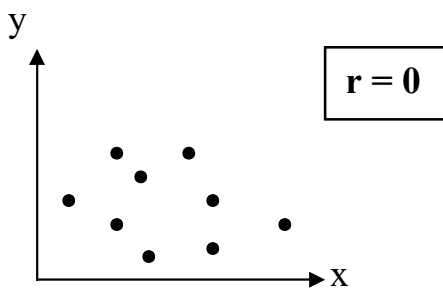
$$y = A + Bx$$

**Correlation Co-efficient ( $r$ )** is the measure of the strength of the relationship between the variables.

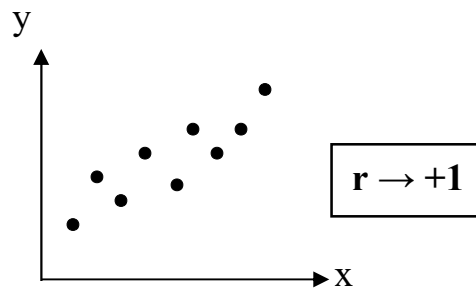
$$-1 \leq r \leq 1$$

Our conclusion for “ $r$ ” always includes strength and direction.

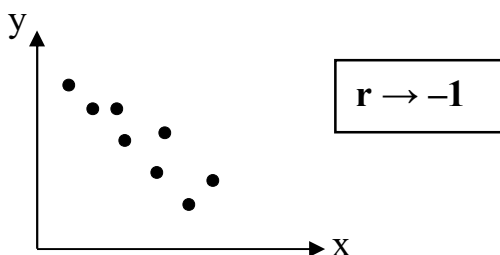
Scatter Plots showing Correlation:



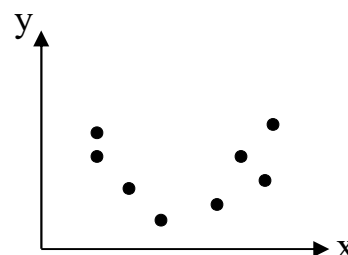
NO RELATIONSHIP BETWEEN X AND Y



STRONG POSITIVE CORRELATION



STRONG NEGATIVE CORRELATION



NON-LINEAR CORRELATION

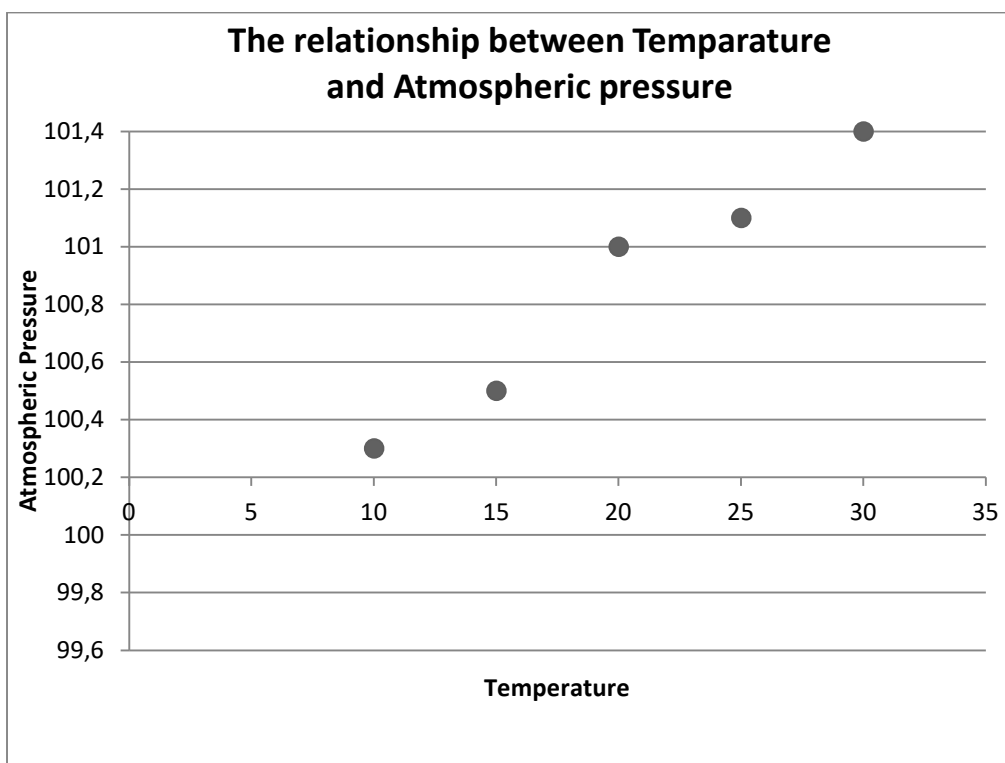


Consider the following table:

Let's investigate whether there is a linear relationship between temperature & atmospheric pressure.

$x$ Temperature (°C)	$y$ Atmospheric pressure (kPa)
10	100,3
15	100,5
20	101,0
25	101,1
30	101,4

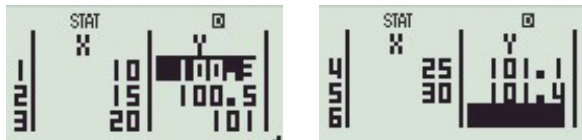
**Pressure is dependent on temperature,**  
so, temperature is the  $x$  variable and pressure the  $y$  variable.



<b>Solution:</b>	<b>Key Sequence:</b>
Set your calculator to Stats mode for Bivariate data	<b>MODE</b> <b>3</b> <b>2</b>

Enter the data into the table:  
Input x-values

Use the [REPLAY] arrows to move the cursor to the y-column.  
Input y-values



1 0 =  
 1 5 =  
 2 0 =  
 2 5 =  
 3 0 =  
 (left arrow) (right arrow)  
 1 0 0 . 3 =  
 1 0 0 . 5 =  
 1 0 1 =  
 1 0 1 . 1 =  
 1 0 1 . 4 =

Clear the screen - ready for the **Regression sub menu**

1:Type    2:Data  
 3:Sum    4:Var  
 5:Reg    6:MinMax

AC    SHIFT 1

### Breakdown of Regression sub menu

Key	Menu Item	Explanation
5: Reg	1:A        2:B 3:r        4:x̂ 5:ŷ	1. Regression co-efficient of A 2. Regression co-efficient of B 3. Correlation co-efficient r 4. Estimated value of x 5. Estimated value of y

#### 1. CORRELATION CO-EFFICIENT

SHIFT 1 5 3 =  $r =$

r is very close to ..... Hence there is a..... **linear correlation** between temperature and atmospheric pressure.

#### 2. CALCULATE A (y intercept) & B (gradient) to determine the line of best fit: $y = A + Bx$

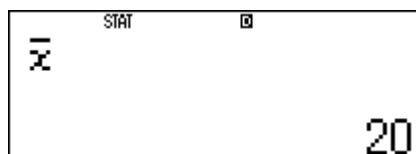
• Calculate A    AC SHIFT 1 5 1 =  $A =$

• Calculate B    AC SHIFT 1 5 2 =  $B =$

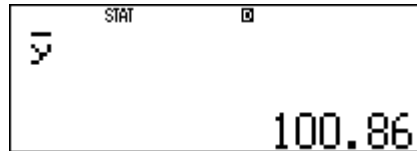
So, the line of best fit is:  $y =$

#### 3. FIND A SECOND POINT TO PLOT THE LINE OF BEST FIT

AC SHIFT 1 4 2 =



AC SHIFT 1 4 5 =



Once you plot the linear equation you can then make projections using your scatter plot.

### HOW TO MAKE PROJECTIONS ON THE CALCULATOR

**RULE:**      **Step 1: Input what is given**  
                 **Step 2: Regression sub menu select which variable is required**

A. What is the approximate temperature if the atmospheric pressure is 100 kPa?

AC 1 0 0 SHIFT 1 5 4 =      100 =

The temperature is.....°C when the pressure is 100 kPa

**Extrapolation: value predicted lies outside the domain and range of the data set given**

B. What is the approximate atmospheric pressure when the temperature is 18°C?

AC 1 8 SHIFT 1 5 5 =      18 =

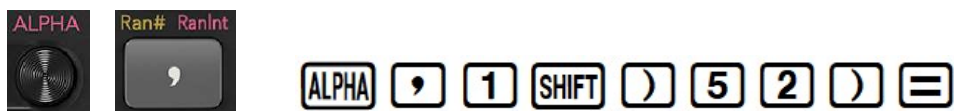
The pressure is.....kPa when the temperature is 18 °C

**Interpolation: value predicted lies within the domain and range of the data set given**

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### SELECTING RANDOM SAMPLES

Let **the calculator** choose a random sample of Integers between 1 and 52, to play the lotto:



**\*NOTE\*** every calculator will give a different string of numbers (Integers are repeated)

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