

## VARIABLE MEMORIES & SOLVING EQUATIONS USING A CASIO SCIENTIFIC CALCULATOR

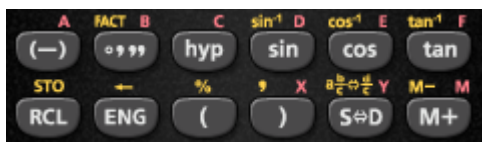
Astrid Scheiber  
CASIO

Adequate knowledge of calculator skills makes the teaching of Financial Maths & Functions easier and enables the educator to assist their learners more efficiently.

**Content:** This workshop will cover: In-putting values into the CASIO calculator MEMORY, using the saved values & recalling what has been saved. Using TABLE MODE – solving Simultaneous, Quadratic & Cubic equations.

**Worksheet:**

### VARIABLE MEMORIES



|   |   |
|---|---|
| To assign the result of $3 + 5$ to variable A | $\boxed{3} \boxed{+} \boxed{5} \boxed{\text{SHIFT}} \boxed{\text{RCL}} \boxed{(-)}$ |
| To multiply the contents of variable A by 10  | $\boxed{\text{ALPHA}} \boxed{(-)} \boxed{\times} \boxed{1} \boxed{0} \boxed{=}$     |
| To recall the contents of variable A          | $\boxed{\text{RCL}} \boxed{(-)}$  |

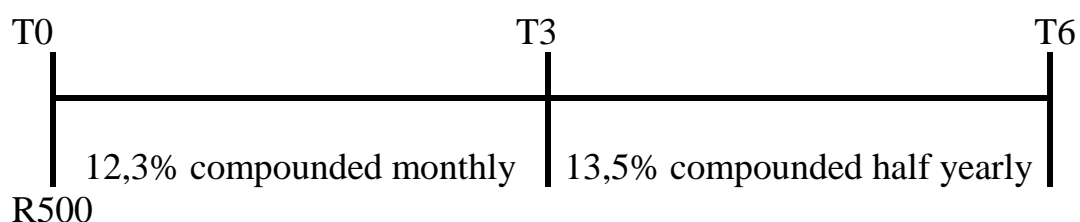
On the calculator, financial maths calculations are done as a continuous calculation.

If you use the memory keys, you do not have to key in the same numbers repeatedly.

Which helps save time and prevent confusion.

#### Example 1

What would an investment of R500 be worth in 6 years' time, if for the first 3 years it earns 12,3% p.a. compounded monthly and for the last 3 years it earns 13,5% p.a. compounded half-yearly?



$$A = P(1 + i)^n$$

$$A = 500 \left(1 + \frac{0.123}{12}\right)^{3 \times 12} \left(1 + \frac{0.135}{2}\right)^{3 \times 2}$$

STORE:  $\left(1 + \frac{0.123}{12}\right)$  INTO VARIABLE A      **SHIFT** **RCL** **(-)**

Calculator display:  $\left(1 + \frac{0.123}{12}\right) \rightarrow A$   
4041  
4000

STORE:  $\left(1 + \frac{0.135}{2}\right)$  INTO VARIABLE B      **SHIFT** **RCL** **0,99**

Calculator display:  $\left(1 + \frac{0.135}{2}\right) \rightarrow B$   
427  
400

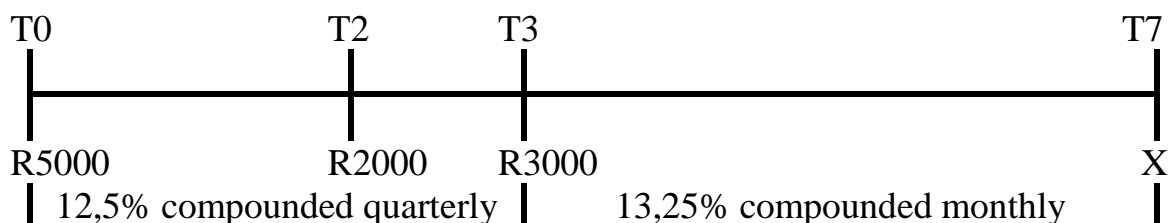
And then complete the calculation

**5** **0** **0** **ALPHA** **(-)** **x<sup>n</sup>** **3** **x** **1** **2** **▶** **ALPHA** **0,99** **x<sup>n</sup>** **3** **x**  
**2**

Calculator display:  $500A^{3 \times 12} B^{3 \times 2}$   
1068.110624

### Example 2

A man borrows R5 000 and agrees to repay the amount as follows: R2 000 after 2 years, R3 000 after 3 years and the balance at the end of 7 years. How much must he pay if interest is at 12,5% p.a. compounded quarterly for the first three years and 13,25% p.a. compounded monthly thereafter?



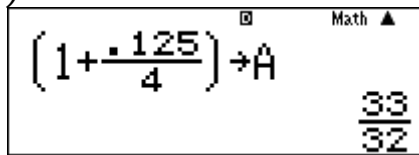
$$A = P(1 + i)^n$$

$$0 = 5000 \left(1 + \frac{0.125}{4}\right)^{3 \times 4} \left(1 + \frac{0.1325}{12}\right)^{4 \times 12}$$

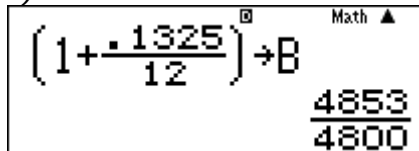
$$- 2000 \left(1 + \frac{0.125}{4}\right)^{1 \times 4} \left(1 + \frac{0.1325}{12}\right)^{4 \times 12}$$

$$- 3000 \left(1 + \frac{0.1325}{12}\right)^{4 \times 12} - X$$

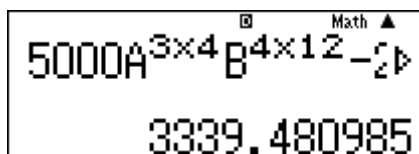
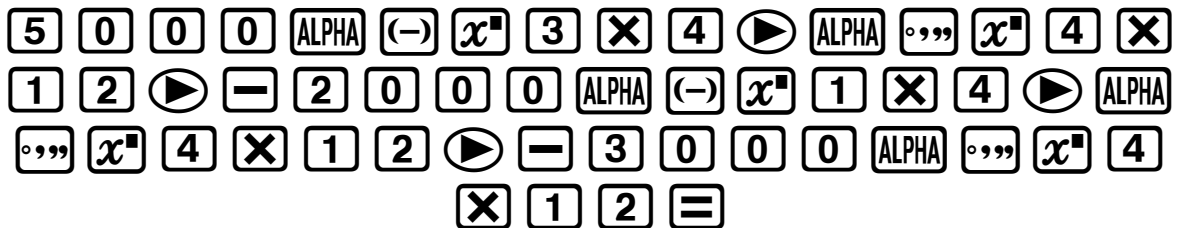
STORE:  $\left(1 + \frac{0.125}{4}\right)$  INTO VARIABLE A      **SHIFT** **RCL** **(-)**



STORE:  $\left(1 + \frac{0.1325}{12}\right)$  INTO VARIABLE B      **SHIFT** **RCL** **o''''**



And then complete the calculation



- The Memory Keys save time – less calculator keys are pressed.
- The Memory Keys do not have to be cleared to be used again. When saving a new value, it overwrites the existing value.

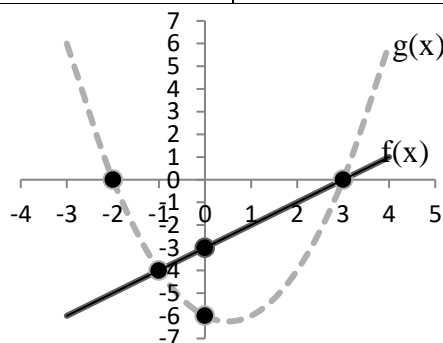
# MODE 3: Table

Find the points of intersection of the straight line  $f(x) = x - 3$  and the parabola  $g(x) = x^2 - x - 6$  when  $x \in [-3 ; 4]$

| <p><b>Key Sequence:</b></p> <ul style="list-style-type: none"> <li>• Input <math>f(x)</math> formula <math>\text{=}</math></li> <li>• Input <math>g(x)</math> formula <math>\text{=}</math></li> <li>• Set boundaries for the table:<br/>             Start? <math>\text{(-)}</math> <math>\text{3}</math> <math>\text{=}</math><br/>             End? <math>\text{4}</math> <math>\text{=}</math><br/>             Step? <math>\text{1}</math> <math>\text{=}</math></li> </ul> <p><b>Point of Intersection (-1 ; -4)</b></p> <p><b>Point of Intersection (3 ; 0)</b></p> | <p><b>On screen:</b></p> <p><math>f(X)=X-3</math></p> <p><math>g(X)=X^2-X-6</math></p> <table border="1"> <thead> <tr> <th>X</th> <th>F(X)</th> <th>G(X)</th> </tr> </thead> <tbody> <tr> <td>-1</td> <td>-4</td> <td>-4</td> </tr> <tr> <td>0</td> <td>-3</td> <td>-6</td> </tr> <tr> <td>1</td> <td>-2</td> <td>-6</td> </tr> <tr> <td>2</td> <td>-1</td> <td>-4</td> </tr> </tbody> </table> <table border="1"> <thead> <tr> <th>X</th> <th>F(X)</th> <th>G(X)</th> </tr> </thead> <tbody> <tr> <td>3</td> <td>0</td> <td>0</td> </tr> </tbody> </table> | X    | F(X) | G(X) | -1 | -4 | -4 | 0 | -3 | -6 | 1 | -2 | -6 | 2 | -1 | -4 | X | F(X) | G(X) | 3 | 0 | 0 |
|--|---|------|------|------|----|----|----|---|----|----|---|----|----|---|----|----|---|------|------|---|---|---|
| X  | F(X)  | G(X) |      |      |    |    |    |   |    |    |   |    |    |   |    |    |   |      |      |   |   |   |
| -1   | -4  | -4   |      |      |    |    |    |   |    |    |   |    |    |   |    |    |   |      |      |   |   |   |
| 0  | -3  | -6   |      |      |    |    |    |   |    |    |   |    |    |   |    |    |   |      |      |   |   |   |
| 1  | -2  | -6   |      |      |    |    |    |   |    |    |   |    |    |   |    |    |   |      |      |   |   |   |
| 2  | -1  | -4   |      |      |    |    |    |   |    |    |   |    |    |   |    |    |   |      |      |   |   |   |
| X  | F(X)  | G(X) |      |      |    |    |    |   |    |    |   |    |    |   |    |    |   |      |      |   |   |   |
| 3  | 0   | 0    |      |      |    |    |    |   |    |    |   |    |    |   |    |    |   |      |      |   |   |   |

**\* ZOOM IN \* and find the turning point of  $g(x)$**

| <p><b>Key Sequence:</b></p> <ul style="list-style-type: none"> <li>• <math>\text{AC}</math></li> <li>• Change the boundaries of the table<br/>             Start? <math>\text{0}</math> <math>\text{=}</math><br/>             End? <math>\text{1}</math> <math>\text{=}</math></li> <li>• Reduce the STEPS/INTERVALS for a more detailed table.<br/>             Step? <math>\text{.}</math> <math>\text{2}</math> <math>\text{5}</math> <math>\text{=}</math></li> </ul> <p><b>Turning point of <math>g(x)</math>: (0,5 ; -6,25)</b></p> | <p><b>On screen:</b></p> <table border="1"> <thead> <tr> <th>X</th> <th>F(X)</th> <th>G(X)</th> </tr> </thead> <tbody> <tr> <td>0.25</td> <td>-2.75</td> <td>-6.1875</td> </tr> <tr> <td>0.5</td> <td>-2.5</td> <td>-6.25</td> </tr> </tbody> </table> <table border="1"> <thead> <tr> <th>X</th> <th>F(X)</th> <th>G(X)</th> </tr> </thead> <tbody> <tr> <td>0.75</td> <td>-2.25</td> <td>-6.1875</td> </tr> <tr> <td>1</td> <td>-2</td> <td>-6</td> </tr> </tbody> </table> | X       | F(X) | G(X) | 0.25 | -2.75 | -6.1875 | 0.5 | -2.5 | -6.25 | X | F(X) | G(X) | 0.75 | -2.25 | -6.1875 | 1 | -2 | -6 |
|--|---|---------|------|------|------|-------|---------|-----|------|-------|---|------|------|------|-------|---------|---|----|----|
| X  | F(X)  | G(X)    |      |      |      |       |         |     |      |       |   |      |      |      |       |         |   |    |    |
| 0.25   | -2.75   | -6.1875 |      |      |      |       |         |     |      |       |   |      |      |      |       |         |   |    |    |
| 0.5  | -2.5  | -6.25   |      |      |      |       |         |     |      |       |   |      |      |      |       |         |   |    |    |
| X  | F(X)  | G(X)    |      |      |      |       |         |     |      |       |   |      |      |      |       |         |   |    |    |
| 0.75   | -2.25   | -6.1875 |      |      |      |       |         |     |      |       |   |      |      |      |       |         |   |    |    |
| 1  | -2  | -6      |      |      |      |       |         |     |      |       |   |      |      |      |       |         |   |    |    |



# SOLVING EQUATIONS

1. Simultaneous equations with 2 unknowns

**Solve for x and y:**

$$3x + 2y = -8$$

$$5x - 4y = -6$$

Manipulate

$$y = \frac{-3x - 8}{2}$$

$$y = \frac{5x + 6}{4}$$

| <p><b>Key Sequence:</b></p> <ul style="list-style-type: none"> <li>Input f(x) formula <math>\boxed{=}</math></li> <li>Input g(x) formula <math>\boxed{=}</math></li> <li>Set boundaries for the table:<br/>           Start? <math>\boxed{=}</math> <math>\boxed{9}</math> <math>\boxed{=}</math><br/>           End? <math>\boxed{9}</math> <math>\boxed{=}</math><br/>           Step? <math>\boxed{1}</math> <math>\boxed{=}</math></li> </ul> <p><math>x = -2</math> and <math>y = -1</math></p> | <p><b>On screen:</b></p> $f(X) = \frac{-3X - 8}{2}$ $g(X) = \frac{5X + 6}{4}$ <table border="1"> <thead> <tr> <th>X</th> <th>F(X)</th> <th>G(X)</th> </tr> </thead> <tbody> <tr> <td>-2</td> <td>-1</td> <td>-1</td> </tr> </tbody> </table> | X    | F(X) | G(X) | -2 | -1 | -1 |
|--|--|------|------|------|----|----|----|
| X  | F(X)   | G(X) |      |      |    |    |    |
| -2   | -1   | -1   |      |      |    |    |    |

*DON'T FORGET*

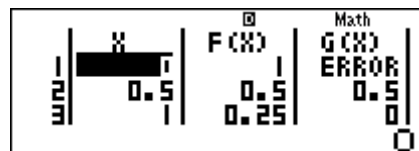
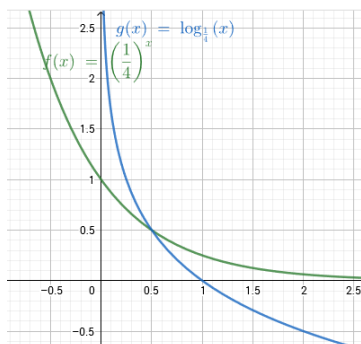
$f(x)$  &  $g(x)$  – 20 x values  
 $f(x)$  – 30 x values

*HOW TO CHANGE:*

|   |  |        |       |        |         |        |       |        |  |  |              |         |               |
|---|--|--------|-------|--------|---------|--------|-------|--------|--|--|--------------|---------|---------------|
| $\boxed{\text{SHIFT}}$ $\boxed{\text{MODE}}$ $\boxed{\blacktriangledown}$ | <table border="1"> <tr> <td>1:ab/c</td> <td>2:d/c</td> </tr> <tr> <td>3:STAT</td> <td>4:TABLE</td> </tr> <tr> <td>5:Disp</td> <td>6:APO</td> </tr> <tr> <td>7:CONT</td> <td></td> </tr> </table> | 1:ab/c | 2:d/c | 3:STAT | 4:TABLE | 5:Disp | 6:APO | 7:CONT |  | <table border="1"> <tr> <td>Select Type?</td> </tr> <tr> <td>1: f(x)</td> </tr> <tr> <td>2: f(x), g(x)</td> </tr> </table> | Select Type? | 1: f(x) | 2: f(x), g(x) |
| 1:ab/c  | 2:d/c  |        |       |        |         |        |       |        |  |  |              |         |               |
| 3:STAT  | 4:TABLE  |        |       |        |         |        |       |        |  |  |              |         |               |
| 5:Disp  | 6:APO  |        |       |        |         |        |       |        |  |  |              |         |               |
| 7:CONT  |  |        |       |        |         |        |       |        |  |  |              |         |               |
| Select Type?  |  |        |       |        |         |        |       |        |  |  |              |         |               |
| 1: f(x)   |  |        |       |        |         |        |       |        |  |  |              |         |               |
| 2: f(x), g(x)   |  |        |       |        |         |        |       |        |  |  |              |         |               |

$\boxed{4}$

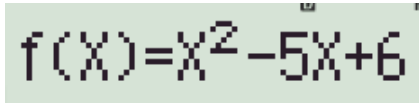
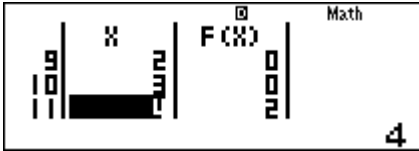
Now try:  $\left(\frac{1}{4}\right)^x = \log_{\frac{1}{4}} x$       Start: 0      End: 9      Steps: 0,5



## 2. Quadratic equation

Generate a TABLE for the equation & read off the  $x$  value where  $f(x) = 0$

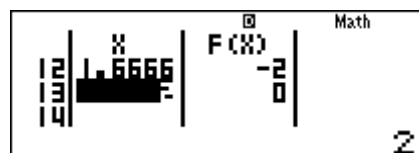
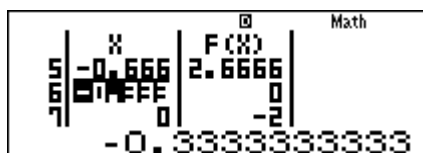
$$x^2 - 5x + 6 = 0$$

|  |   |
|--|---|
| <p><b>Key Sequence:</b></p> <ul style="list-style-type: none"> <li>Input <math>f(x)</math> equation <math>\text{=}</math><br/> <b>to input the variable <math>x</math>:</b><br/> <math>\text{ALPHA}</math> <math>\text{)</math></li> <li><math>g(x) =</math> <math>\text{=}</math></li> <li>Set boundaries for your table:<br/> <b>Start?</b> <math>\text{-}</math> <math>\text{6}</math> <math>\text{=}</math><br/> <b>End?</b> <math>\text{6}</math> <math>\text{=}</math><br/> <b>Step?</b> <math>\text{1}</math> <math>\text{=}</math></li> </ul> <p><math>f(x) = 0</math> at <math>x = 2</math> or <math>x = 3</math></p> | <p><b>On screen:</b></p> <br> |
|--|---|

**DOMAIN:** Negative & positive values of the constant

**STEPS:** Reciprocal of the co-efficient of the highest power of  $x$

Now try:  $3x^2 - 5x = 2$



## 3. Cubic equation

Generate a TABLE for the equation & read off the  $x$  value where  $f(x) = 0$

$$2x^3 + 3x^2 - 11x - 6 = 0$$

**Key Sequence:**

- Input  $f(x)$  equation  $\equiv$
- $g(x) = \equiv$
- Set boundaries for your table:

Start?  $\boxed{-}$   $\boxed{6}$   $\equiv$

End?  $\boxed{6}$   $\equiv$

Step?  $\boxed{1}$   $\boxed{\frac{\square}{\square}}$   $\boxed{2}$   $\equiv$

- Turn  $g(x)$  off

$\boxed{\blacktriangleright}$   $\boxed{\text{SHIFT}}$   $\boxed{\text{MODE}}$   $\boxed{\blacktriangledown}$   $\boxed{4}$   $\boxed{1}$

$f(x) = 0$  at

$$x = -3 \text{ or } x = -\frac{1}{2} \text{ or } x = 2$$

**On screen:**

$$f(x) = X^2 - 11X - 6$$

Math  
Insufficient MEM  
[AC] :Cancel  
[←][→]:Goto

| X | F(X)  |
|---|-------|
| 6 | -16.5 |
| 7 | 0     |
| 8 | 9     |

-3

| X  | F(X) |
|----|------|
| 11 | 6    |
| 12 | -6   |
| 13 | 0    |

-0.5

| X  | F(X) |
|----|------|
| 16 | -9   |
| 17 | 0    |
| 18 | 16.5 |

2

Now try:  $x^3 - \frac{3}{2}x^2 - 4x + 6 = 0$

| X  | F(X) |
|----|------|
| 8  | -18  |
| 9  | 0    |
| 10 | 10.5 |

-2

| X  | F(X) |
|----|------|
| 15 | 0    |
| 16 | 0    |
| 17 | 0    |

1.5

| X  | F(X) |
|----|------|
| 16 | 0    |
| 17 | 0    |
| 18 | 4.5  |

2

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